

# Package ‘spatialfusion’

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**Suggests** INLA, geoR, SDraw, testthat, tmap, R.rsp

**Depends** R (>= 3.4.0), Rcpp

**Type** Package

**VignetteBuilder** R.rsp

**Additional\_repositories** <https://inla.r-inla-download.org/R/stable/>

**Title** Multivariate Analysis of Spatial Data Using a Unifying Spatial Fusion Framework

**Version** 0.6-5

**Date** 2022-01-24

**Maintainer** Craig Wang <craigwang247@gmail.com>

**Description** Multivariate modelling of geostatistical (point), lattice (areal) and point pattern data in a unifying spatial fusion framework. Details are given in Wang and Furrer (2021) <[doi:10.1016/j.csda.2021.107240](https://doi.org/10.1016/j.csda.2021.107240)>. Model inference is done using either 'Stan' <<https://mc-stan.org/>> or 'INLA' <<https://www.r-inla.org/>>.

**License** GPL (>= 3)

**Encoding** UTF-8

**LazyData** TRUE

**NeedsCompilation** no

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spatialfusion-package *Multivariate Analysis of Spatial Data Using a Unifying Spatial Fusion Framework*

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## Description

Multivariate modelling of geostatistical (point), lattice (areal) and point pattern data in a unifying spatial fusion framework. Details are given in Wang and Furrer (2021) <doi: [10.1016/j.csda.2021.107240](https://doi.org/10.1016/j.csda.2021.107240)>. Model inference is done using either 'Stan' <<https://mc-stan.org/>> or 'INLA' <<https://www.r-inla.org/>>.

## Details

Package:	spatialfusion
Type:	Package
Version:	0.6-5
Date:	2022-01-24
License:	GPL (>= 3)
LazyLoad:	yes

## Data analysis pipeline

**Preparing data:** `fusionData()` is used to set up the data structure needed for spatial fusion modelling. Depending on the chosen 'method', either a `dstan` or a `dinla` object is returned. This object is then supplied to the 'data' argument in `fusion()` for fitting a spatial fusion model. In terms of the 'method', Stan provides Hamiltonian Monte Carlo-based full Bayesian inference, while INLA provides approximate Bayesian inference at a much faster computation speed. Their results are very similar in our simulation studies (Wang and Furrer, 2021 <doi: [10.1016/j.csda.2021.107240](https://doi.org/10.1016/j.csda.2021.107240)>).

**IMPORTANT:** Users should be familiar with either **rstan** or **INLA** packages themselves. For Stan, users should know how to choose priors appropriately. For INLA, users should know how

to set up an appropriate mesh.

**Fitting model:** `fusion()` is used to fit a spatial fusion model. The most related publication is by Wang and Furrer (2021) <doi: [10.1016/j.csda.2021.107240](https://doi.org/10.1016/j.csda.2021.107240)>, which introduced the framework.

We suggest users to test their model on smaller sub-sampled dataset first, to check model fitting issues such as convergence, identifiability etc. It also helps to get an idea of the computation time required. Afterwards, users can fit the model to their full dataset. The output has a class `fusionModel`.

**Model diagnostics:** Common generic functions such as `fitted()`, `predict()`, `summary()` and `plot()` are available for `fusionModel` objects. Diagnostics of spatial fusion models should be done in the same way as for a Stan or a INLA model, depending on the chosen method.

### Author(s)

Craig Wang <[craigwang247@gmail.com](mailto:craigwang247@gmail.com)>

### Examples

```
## Citations
citation('spatialfusion')

## Vignette: short demo
vignette("spatialfusion_vignette", package = "spatialfusion")
```

---

dataDomain

*Municipality map for Canton of Zurich*

---

### Description

This dataset gives the municipality (gemeinde) map for the Canton of Zurich in Switzerland as of 2019, consisting of 162 municipalities.

### Usage

```
dataDomain
```

### Format

A `SpatialPolygons` object containing 162 Polygons.

### References

<https://www.zh.ch/de/politik-staat/statistik-daten.html> (Visited: 26/06/2021)

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dataGeo	<i>Simulated geostatistical data</i>
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**Description**

This dataset gives simulated geostatistical data at 200 locations with a normal-distributed response variable and a covariate.

**Usage**

dataGeo

**Format**

A `SpatialPointsDataFrame` containing 200 observations with “lungfunction” as the response variable and a “covariate”.

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dataLattice	<i>Simulated lattice data</i>
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**Description**

This dataset gives simulated lattice data at 162 areas with a Poisson-distributed response variable, a covariate and an offset term. It has the same set of polygons as `dataDomain`.

**Usage**

dataLattice

**Format**

A `SpatialPolygonsDataFrame` containing 162 observations with “mortality” as the response variable, a “covariate” and a “pop” as the population offset term.

**See Also**

[dataDomain](#)

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dataPP	<i>Simulated point pattern data</i>
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**Description**

This dataset gives the coordinates of 116 events.

**Usage**

```
dataPP
```

**Format**

A `SpatialPoints` containing 116 locations with events.

---

fitted	<i>Obtain fitted values of spatial fusion model</i>
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---

**Description**

Generate fitted values of the response variables based on a spatial fusion model.

**Usage**

```
## S3 method for class 'fusionModel'
fitted(object, type = c("link", "summary", "full", "latent"), ...)
```

**Arguments**

object	object of class <code>fusionModel</code> . Output of <code>fusion()</code> .
type	string. The default "link" gives the median of linear predictors; "summary" gives the mean, standard deviation and quantiles of linear predictors; "full" gives full marginals for INLA or posterior samples for Stan; "latent" gives the median of latent processes with their corresponding locations.
...	additional arguments not used.

**Details**

For INLA models, no posterior values for point pattern data will be generated.

**Value**

The returned value is a list containing the fitted results for each response variable.

**Author(s)**

Craig Wang

**See Also**[fusion](#), [fusion.dinla](#), [fusion.dstan](#).**Examples**

```
## example based on simulated data
## Not run:
if (require("INLA", quietly = TRUE) & require("SDraw", quietly = TRUE)) {
  dat <- fusionSimulate(n.point = 20, n.area = 10, n.grid = 2,
    psill = 1, phi = 1, nugget = 0, tau.sq = 0.5,
    point.beta = list(rbind(1,5)),
    area.beta = list(rbind(-1, 0.5)),
    distributions = c("normal", "poisson"),
    design.mat = matrix(c(1,1,1)))

  geo_data <- data.frame(x = dat$mrf[dat$sample.ind, "x"],
    y = dat$mrf[dat$sample.ind, "y"],
    cov.point = dat$data$X_point[,2],
    outcome = dat$data$Y_point[[1]])
  lattice_data <- sp::SpatialPolygonsDataFrame(dat$poly,
    data.frame(outcome = dat$data$Y_area[[1]],
    cov.area = dat$data$X_area[,2]))

  dat_inla <- fusionData(geo.data = geo_data, geo.formula = outcome ~ cov.point,
    lattice.data = lattice_data, lattice.formula = outcome ~ cov.area,
    pp.data = dat$data$lgcp.coords[[1]],
    distributions = c("normal", "poisson"),
    method = "INLA")

  mod_inla <- fusion(data = dat_inla, n.latent = 1, bans = 0,
    prior.range = c(1, 0.5), prior.sigma = c(1, 0.5),
    mesh.locs = dat_inla$locs_point, mesh.max.edge = c(0.5, 1))

  fit_inla <- fitted(mod_inla, type = "summary")
}

## End(Not run)
```

fusion

*Fit a spatial fusion model***Description**

Fit a spatial fusion model based on the unifying framework proposed by Wang and Furrer (2021). One or more latent Gaussian process(es) is assumed to be associated with the spatial response variables.

## Usage

```
fusion(data, n.latent = 1, bans = 0, pp.offset,  
       verbose = FALSE, ...)
```

## Arguments

<code>data</code>	an object of class either <code>dstan</code> or <code>dinla</code> . Output of <code>fusionData()</code> .
<code>n.latent</code>	integer. Number of latent processes to be modeled.
<code>bans</code>	either 0 or a matrix of 0s and 1s with dimension J times <code>n.latent</code> , where J is the total number of response variables. If <code>matrix</code> , 1 indicates banning an association between the latent process and response variable. If 0, no association is banned.
<code>pp.offset</code>	numeric, vector of numeric or matrix of numeric. Offset term for point pattern data.
<code>verbose</code>	logical. If TRUE, prints progress and debugging information.
<code>...</code>	additional arguments depending on the class of data

## Details

It is not possible to add covariates for point pattern data. However, an offset term can be supplied. Any covariate information can be taken into account by firstly fit a fixed effect model and enter the fitted values into the offset term as `pp.offset`.

## Value

The returned value is a named list of class `fusionModel` consisting of model output and data structure used. If the model is fitted with INLA, the mesh used is also included.

## Author(s)

Craig Wang

## References

Wang, C., Furrer, R. and for the SNC Study Group (2021). Combining heterogeneous spatial datasets with process-based spatial fusion models: A unifying framework, *Computational Statistics & Data Analysis*

## See Also

`fusion.dinla`, `fusion.dstan`, `fusionData` for preparing data, `fitted.fusionModel` for extracting fitted values, `predict.fusionModel` for prediction.

**Examples**

```

## example based on simulated data

if (require("geoR", quietly = TRUE)) {
  dat <- fusionSimulate(n.point = 20, n.area = 10, n.grid = 2,
    psill = 1, phi = 1, nugget = 0, tau.sq = 0.5,
    point.beta = list(rbind(1,5)),
    area.beta = list(rbind(-1, 0.5)),
    distributions = c("normal", "poisson"),
    design.mat = matrix(c(1,1,1)))

  geo_data <- data.frame(x = dat$mrfs[dat$sample.ind, "x"],
    y = dat$mrfs[dat$sample.ind, "y"],
    cov.point = dat$data$X_point[,2],
    outcome = dat$data$Y_point[[1]])
  lattice_data <- sp::SpatialPolygonsDataFrame(dat$poly,
    data.frame(outcome = dat$data$Y_area[[1]],
    cov.area = dat$data$X_area[,2]))

  dat_stan <- fusionData(geo.data = geo_data, geo.formula = outcome ~ cov.point,
    lattice.data = lattice_data, lattice.formula = outcome ~ cov.area,
    pp.data = dat$data$lgcp.coords[[1]], distributions = c("normal", "poisson"),
    method = "Stan")

  ## S3 method for class 'dstan'
  mod_stan <- fusion(data = dat_stan, n.latent = 1, bans = 0, pp.offset = 1,
    prior.phi = list(distr = "normal", pars = c(1, 10)))
  summary(mod_stan)
}

## Not run:
if (require("INLA", quietly = TRUE)) {
  dat_inla <- fusionData(geo.data = geo_data, geo.formula = outcome ~ cov.point,
    lattice.data = lattice_data, lattice.formula = outcome ~ cov.area,
    pp.data = dat$data$lgcp.coords[[1]], distributions = c("normal", "poisson"),
    method = "INLA")

  ## S3 method for class 'dinla'
  mod_inla <- fusion(data = dat_inla, n.latent = 1, bans = 0,
    prior.range = c(1, 0.5), prior.sigma = c(1, 0.5),
    mesh.locs = dat_inla$locs_point, mesh.max.edge = c(0.5, 1))
  summary(mod_inla)
}

## End(Not run)

```



## Description

Fit a spatial fusion model using INLA based on the unifying framework proposed by Wang and Furrer (2021). One or more latent Gaussian process(es) is assumed to be associated with the spatial response variables.

## Usage

```
## S3 method for class 'dinla'
fusion(data, n.latent = 1, bans = 0, pp.offset,
        verbose = FALSE, alpha = 3/2, prior.range,
        prior.sigma, prior.args, mesh.locs, mesh.max.edge,
        mesh.args, inla.args, ...)
```

## Arguments

data	an object of class <code>dinla</code> . Output of <code>fusionData()</code> .
n.latent	integer. Number of latent processes to be modeled.
bans	either 0 or a matrix of 0s and 1s with dimension J times n.latent, where J is the total number of response variables. If matrix, 1 indicates banning an association between the latent process and response variable. If 0, no association is banned.
pp.offset	numeric, vector of numeric or matrix of numeric. Offset term for point pattern data.
verbose	logical. If TRUE, prints progress and debugging information
alpha	numeric between 0 and 2. Determines the covariance model, defined as $\nu + 1$ for two dimensional space. Default value is 3/2 which corresponds to the exponential covariance model. See details.
prior.range	vector of length 2, with (range0, Prange) specifying that $P(\rho\sqrt{8\nu} < \text{range0}) = \text{Prange}$ , where $\rho\sqrt{8\nu}$ is the practical spatial range of the random field. If Prange is NA, then range0 is used as a fixed range value. See details.
prior.sigma	vector of length 2, with (sigma0, Psigma) specifying that $P(\sigma > \text{sigma0}) = \text{Psigma}$ , where $\sigma$ is the marginal standard deviation of the field. If Psigma is NA, then sigma0 is used as a fixed sigma value. See details.
prior.args	named list. Other prior arguments for <code>inla.spde2.matern()</code> in <b>INLA</b> .
mesh.locs	matrix with two columns, or a <code>SpatialPoints</code> , <code>SpatialPointsDataFrame</code> object. Locations to be used as initial triangulation nodes.
mesh.max.edge	vector of length one or two. The largest allowed triangle edge length for inner (and optional outer extension) mesh.
mesh.args	named list. Other mesh arguments passed to <code>inla.mesh.2d()</code> in <b>INLA</b> .
inla.args	named list. Other inla arguments passed to <code>inla()</code> <b>INLA</b> .
...	additional arguments not used

## Details

The prior used for modeling the latent spatial processes is `inla.spde2.matern`. Each spatial component is named as `sij`, where `i` denotes the `i`th latent process and `j` denotes the `j`th variable. For example, `s12` is the first latent process that is associated with the second variable. The first variable (with the following ordering: geostatistical, lattice, point pattern data) that a spatial component is associated with will have the original component, then the subsequent spatial components associated with other variables are treated as 'copies' of the original component modified by a coefficient `Beta`, as one of the latent parameters.

The INLA approximation only works for Matern covariance function, which can be written as

$$C(d) = \sigma^2 / (2^{\nu-1} \Gamma(\nu)) * (d\sqrt{2\nu/\rho})^\nu K_\nu(d\sqrt{2\nu/\rho}),$$

where  $d$  is the Euclidean distance,  $K_\nu$  is a modified Bessel function,  $\rho$  is the spatial range,  $\sigma^2$  is the partial sill and  $\nu$  is the smoothness parameter. NOTE: the range parameter in INLA output is defined as "practical range" as  $\rho\sqrt{8\nu}$ .

## Value

The returned value is a list consists of

<code>model</code>	an object of class <code>inla</code> representing the fitted INLA model
<code>mesh</code>	an object of class <code>inla.mesh</code> containing the mesh used.
<code>data</code>	the data structure used to fit the model

## Author(s)

Craig Wang

## References

Wang, C., Furrer, R. and for the SNC Study Group (2021). Combining heterogeneous spatial datasets with process-based spatial fusion models: A unifying framework, *Computational Statistics & Data Analysis*

## See Also

[fusionData](#) for preparing data, [fitted](#) for extracting fitted values, [predict](#) for prediction.

## Examples

```
## example based on simulated data
## Not run:
if (require("INLA", quietly = TRUE) & require("SDraw", quietly = TRUE)) {
  dat <- fusionSimulate(n.point = 50, n.area = 20, n.grid = 4,
    psill = 1, phi = 1, nugget = 0, tau.sq = 0.5,
    point.beta = list(rbind(1,5)),
    area.beta = list(rbind(-1, 0.5)),
    distributions = c("normal", "poisson"),
    design.mat = matrix(c(1,1,1)))

  geo_data <- data.frame(x = dat$mrf[dat$sample.ind, "x"],
```

```

      y = dat$mrf[dat$sample.ind, "y"],
      cov.point = dat$data$X_point[,2],
      outcome = dat$data$Y_point[[1]])
lattice_data <- sp::SpatialPolygonsDataFrame(dat$poly,
      data.frame(outcome = dat$data$Y_area[[1]],
      cov.area = dat$data$X_area[,2]))

dat_inla <- fusionData(geo.data = geo_data, geo.formula = outcome ~ cov.point,
      lattice.data = lattice_data, lattice.formula = outcome ~ cov.area,
      pp.data = dat$data$lgcp.coords[[1]], distributions = c("normal", "poisson"),
      method = "INLA")

mod_inla <- fusion(data = dat_inla, n.latent = 1, bans = 0,
      prior.range = c(1, 0.5), prior.sigma = c(1, 0.5),
      mesh.locs = dat_inla$locs_point, mesh.max.edge = c(0.5, 1))

summary(mod_inla)
}

## End(Not run)

```

---

fusion.dstan

*Fit a spatial fusion model using Stan*


---

## Description

Fit a spatial fusion model using Stan based on the unifying framework proposed by Wang and Furrer (2021). One or more latent Gaussian process(es) is assumed to be associated with the spatial response variables.

## Usage

```

## S3 method for class 'dstan'
fusion(data, n.latent = 1, bans = 0, pp.offset,
      verbose = FALSE, prior.pointbeta, prior.areabeta,
      prior.tausq, prior.phi, prior.z,
      nsamples = 2000, nburnin = 1000, thinning = 1,
      nchain = 2, ncore = 2, adapt.delta = 0.95, ...)

```

## Arguments

data	an object of class <code>dstan</code> . Output of <code>fusionData()</code> .
n.latent	integer. Number of latent processes to be modeled.
bans	either 0 or a matrix of 0s and 1s with dimension J times n.latent, where J is the total number of response variables. If matrix, 1 indicates banning an association between the latent process and response variable. If 0, no association is banned.
pp.offset	numeric, vector of numeric or matrix of numeric. Offset term for point pattern data.

verbose	logical. If TRUE, prints progress and debugging information.
prior.pointbeta	a list with prior information for the coefficients of geostatistical model component. The default prior is <code>list(distr = "normal", pars=c(0,10))</code> , i.e. a normal distribution with mean 0 and standard deviation 10.
prior.areabeta	a list with prior information for the coefficients of lattice model component. The default prior is <code>list(distr = "normal", pars=c(0,10))</code> , i.e. a normal distribution with mean 0 and standard deviation 10.
prior.tausq	a list with prior information for the coefficients of geostatistical model component. The default prior is <code>list(distr = "inv_gamma", pars=c(2,1))</code> , i.e. a inverse gamma distribution with shape 2 and rate 1.
prior.phi	a list with prior information for the spatial range parameter. NO default prior is available. We recomend using a moderately informative normal prior.
prior.z	a list with prior information for the design matrix, which also controls the partial sill. The default prior is <code>list(distr = "normal", pars=c(1,1))</code> , i.e. a normal distribution with mean 1 and standard deviation 1.
nsamples	a positive integer specifying the number of samples for each chain (including burn-in samples). Default 2000.
nburnin	a positive integer specifying the number of burn-in samples. Default 1000.
thinning	a positive integer specifying the thinning parameter. Default 1.
nchain	a positive integer specifying the number of chains. Default 2.
ncore	a positive integer specifying the number of cores to use when executing the chains in parallel. Default 2.
adapt.delta	a numeric value between 0 and 1 specifying the target acceptance rate. Default 0.95.
...	additional arguments passed to sampling function in <b>rstan</b>

### Details

In the model parameterization, beta are fixed-effect coefficients, phi is the range parameter,  $Z_{ij}$  is the  $i$ th row and  $j$  column of the design matrix for latent processes and tau\_sq is the variance parameter of a normal distribution.

NOTE: Only exponential covariance model for the latent processes is implemented. However, it can be easily extended by modifying the model code from the output.

### Value

The returned value is a list consists of

model	an object of S4 class <code>stanfit</code> representing the fitted Stan model
data	the data structure used to fit the model

### Author(s)

Craig Wang

## References

Wang, C., Furrer, R. and for the SNC Study Group (2021). Combining heterogeneous spatial datasets with process-based spatial fusion models: A unifying framework, *Computational Statistics & Data Analysis*

## See Also

[fusion.dinla](#), [fusion.dstan](#), [fusionData](#) for preparing data, [fitted.fusionModel](#) for extracting fitted values, [predict.fusionModel](#) for prediction.

## Examples

```
## example based on simulated data

if (require("geoR", quietly = TRUE) & require("SDraw", quietly = TRUE)) {
  dat <- fusionSimulate(n.point = 20, n.area = 10, n.grid = 2,
    psill = 1, phi = 1, nugget = 0, tau.sq = 0.5,
    point.beta = list(rbind(1,5)),
    area.beta = list(rbind(-1, 0.5)),
    distributions = c("normal", "poisson"),
    design.mat = matrix(c(1,1,1)))

  geo_data <- data.frame(x = dat$mrf[dat$sample.ind, "x"],
    y = dat$mrf[dat$sample.ind, "y"],
    cov.point = dat$data$X_point[,2],
    outcome = dat$data$Y_point[[1]])
  lattice_data <- sp::SpatialPolygonsDataFrame(dat$poly,
    data.frame(outcome = dat$data$Y_area[[1]],
    cov.area = dat$data$X_area[,2]))

  dat_stan <- fusionData(geo.data = geo_data, geo.formula = outcome ~ cov.point,
    lattice.data = lattice_data, lattice.formula = outcome ~ cov.area,
    pp.data = dat$data$lgcp.coords[[1]], distributions = c("normal", "poisson"),
    method = "Stan")

  mod_stan <- fusion(data = dat_stan, n.latent = 1, bans = 0, pp.offset = 1,
    prior.phi = list(distr = "normal", pars = c(1, 10)))

  summary(mod_stan)
  # To kill parallel process except one (for stopping a stan call)
  # system("killall R")
}
```

**Description**

Takes various datasets and formulas from different spatial data types and process them to prepare for spatial fusion modeling using either Stan or INLA.

**Usage**

```
fusionData(geo.data, geo.formula,
           lattice.data, lattice.formula,
           pp.data, distributions, domain = NULL,
           method = c("Stan", "INLA"),
           proj4string = CRS(as.character(NA)),
           stan.control = NULL)
```

**Arguments**

geo.data	an object of class <a href="#">data.frame</a> or <a href="#">SpatialPointsDataFrame</a> . If <a href="#">data.frame</a> , it must have column names "x" and "y" as coordinates of observations.
geo.formula	an object of class <a href="#">formula</a> . A symbolic description of the model to be fitted for geostatistical data. For multivariate geostatistical data, use syntax <code>cbind(y1,y2)</code> followed by <code>~</code> .
lattice.data	an object of class <a href="#">SpatialPolygonsDataFrame</a> . Contains lattice data.
lattice.formula	an object of class <a href="#">formula</a> . A symbolic description of the model to be fitted for lattice data. For multivariate lattice data, use syntax <code>cbind(y1,y2)</code> followed by <code>~</code> .
pp.data	an object of class <a href="#">data.frame</a> , <a href="#">SpatialPoints</a> or <a href="#">SpatialPointsDataFrame</a> , or a list of them. If <a href="#">data.frame</a> , it must have column names "x" and "y" as coordinates.
distributions	a vector of strings. Specifying the distributions of each geostatistical and lattice response variable, currently "Gaussian" or "normal", "Poisson" (count) and "Bernoulli" (binary) are supported. Note: no distribution is required to be specified for point pattern data.
domain	an object of class <a href="#">SpatialPolygons</a> . The spatial domain considered for computing gridded point pattern data. If <code>NULL</code> , a bounding box that contains all spatial units is used.
method	character. Either 'Stan' or 'INLA', the method to be used for fitting the spatial fusion model later.
proj4string	projection string of class <a href="#">CRS-class</a> .
stan.control	a named list of parameters to control the Stan implementation of spatial fusion models. Default to <code>NULL</code> such that all the default values are used. <ul style="list-style-type: none"> <li>• <code>n.neighbor</code> (positive integer) Number of nearest neighbors to consider. Default to 5.</li> <li>• <code>n.sampling</code> (positive integer) Number of sampling points for each area. Default to 5.</li> <li>• <code>n.grid</code> (positive integer) Number of grid used to divide the spatial domain in each of x- and y-direction to count the number of cases/events in each grid. Default to 10.</li> </ul>

## Details

It is not possible to add covariate for point pattern data in the spatial fusion framework. However, an offset term can be supplied to `pp.offset` in the modelling stage with `fusion`. Any covariate information can be taken into account by firstly fit a fixed effect model and enter the fitted values into the offset term.

## Value

The returned value is an object of either class `dstan` or `dinla`, depending on the chosen method. They are both lists that contain:

<code>distributions</code>	distribution specified each response variable.
<code>n_point</code>	sample size for geostatistical data.
<code>n_area</code>	sample size for lattice data.
<code>n_grid</code>	Set to 1 for INLA, set to the number of grids for Stan.
<code>p_point</code>	number of coefficients for geostatistical model component (only if there is geostatistical data).
<code>n_point_var, n_area_var, n_pp_var</code>	number of response variables for each data type.
<code>Y_point</code>	response variable for geostatistical data (only if there is geostatistical data).
<code>X_point</code>	covariates for geostatistical data (only if there is geostatistical data).
<code>p_area</code>	number of coefficients for lattice model component (only if there is lattice data).
<code>Y_area</code>	response variable for lattice data (only if there is lattice data).
<code>X_area</code>	covariates for lattice data (only if there is lattice data).
<code>geo.formula, lattice.formula</code>	formulas used for geostatistical and lattice data.

`dstan` additionally contains:

<code>n_neighbor</code>	number of nearest neighbors to consider for NNGP modelling.
<code>n_sample</code>	total number of sampling points.
<code>nearid, nearind_sample</code>	vectors containing neighborhood indices
<code>C_nei, C_site_nei, sC_nei, sC_site_nei</code>	various distance matrices
<code>A1</code>	aggregation matrix that maps sampling points to areal averages (only if there is lattice data).
<code>Y_pp</code>	the number of cases/events in each grid for point pattern data (only if there is point pattern data).
<code>area</code>	the area of each grid (only if there is point pattern data).
<code>grd_lrg</code>	the grid generated for point pattern data modeling (only if there is point pattern data).
<code>locs</code>	all the locations where the latent components are modelled.

dinla additionally contains:

domain	spatial domain as a <a href="#">SpatialPolygons-class</a>
locs_point	locations of geostatistical data.
locs_pp	locations of point pattern data.
poly	lattice data as a <a href="#">SpatialPolygonsDataFrame-class</a> .

### Author(s)

Craig Wang

### See Also

[fusion.dinla](#), [fusion.dstan](#)

### Examples

```
## example based on simulated built-in data

dat <- fusionData(dataGeo, lungfunction ~ covariate,
  dataLattice, mortality ~ covariate,
  dataPP, distribution = c("normal", "poisson"),
  domain = dataDomain,
  method = "INLA")

## Not run:
if (require("INLA", quietly = TRUE)) {
  ## fit a spatial fusion model on the prepared data
  ## pp.offset = 400 was chosen based on simulation parameters
  mod <- fusion(data = dat, n.latent = 1, bans = 0, pp.offset = 400,
    prior.range = c(0.1, 0.5), prior.sigma = c(1, 0.5),
    mesh.locs = dat$locs_point, mesh.max.edge = c(0.5, 1))

  ## parameter estimates
  summary(mod)
}

## End(Not run)
```

---

fusionSimulate

*Simulate spatial data*

---

### Description

Simulate spatial response variables with different data types, including geostatistical (point), lattice (areal), and point pattern data. They share common latent Gaussian processes. The geostatistical and lattice response variables are allowed to have fixed effects.



**Usage**

```
fusionSimulate(n.point, n.area, n.grid, n.pred, dimension = 10,
              psill = 5, phi = 1, nugget = 0, tau.sq = 1,
              domain = NULL, point.beta = NULL, area.beta = NULL,
              nvar.pp = 1, distributions,
              design.mat = matrix(c(1, 1.5, 2)),
              pp.offset, seed)
```

**Arguments**

n.point	positive integer. Sample size for geostatistical (point) data.
n.area	positive integer. Sample size for lattice (areal) data.
n.grid	positive integer. Number of grid to be divided in each direction of the spatial domain.
n.pred	positive integer. Number of prediction locations to sample regularly.
dimension	positive integer. Dimension of the square spatial domain.
domain	an object of class <code>SpatialPolygons</code> or <code>SpatialPolygonsDataFrame</code> . The spatial domain considered for the simulation. If <code>NULL</code> , a square domain with length <code>dimension</code> is used.
psill	positive numeric or numeric vector. Partial sill parameter(s) of the latent Gaussian process(es).
phi	positive numeric or numeric vector. Range parameter(s) of the latent Gaussian process(es).
nugget	positive numeric vector. Nugget parameter(s) of the latent Gaussian process(es).
tau.sq	positive numeric vector. Variance component(s) for normally distributed responses.
point.beta	a list of column matrices. Regression coefficient for geostatistical data, e.g. <code>list(rbind(1,2,3),rbind(2,4,6))</code> for two geostatistical response variables with an intercept plus two covariates each.
area.beta	a list of column matrices. Regression coefficient for lattice data, e.g. see above.
nvar.pp	numeric. Number of point pattern response variables to simulate.
distributions	character vector. Names of distributions for each dependent variables with geostatistical and lattice type, currently “Gaussian” or “normal”, “Poisson” (count) and “Bernoulli” (binary) are supported. Note: no distribution for point pattern data is required to be specified.
design.mat	matrix. Design matrix for the latent Gaussian process(es), with the number of columns equal to the number of latent processes.
pp.offset	numeric. A single offset term for the intensity of point pattern data.
seed	integer. Random seed.

**Details**

The exponential covariance model is used,

$$C(d) = \sigma^2 \exp -d/\phi$$

where  $d$  is the Euclidean distance,  $\sigma^2$  is the partial sill and  $\phi$  is the spatial range.

If the purpose is to validate a fitted latent spatial components of a spatial fusion model, one can check the fitted latent values against `mrff[sample.ind, -1:2]`. If the purpose is to investigate prediction performance of latent spatial components, one can predict at locations `pred.loc` and check against `mrff[pred.ind, -1:2]`.

**Value**

The returned value is a list that consists of:

<code>data</code>	a named list providing data variables.
<code>mrff</code>	a data.frame of locations and the latent Gaussian process.
<code>domain</code>	a SpatialPolygons for the whole domain.
<code>pred.loc</code>	a data.frame of locations for prediction.
<code>pred.ind</code>	a vector of indices for prediction locations.
<code>sample.ind</code>	a vector providing the indices of sampled locations in the Gaussian process. (only if there is geostatistical data)
<code>mean.w</code>	a list of aggregated latent process for each area. (only if there is lattice data)
<code>poly</code>	a SpatialPolygonDataFrame for the lattice data. (only if there is lattice data)
<code>lgcp.grid</code>	a data.frame containing the centroids of gridded cells for point pattern data and the corresponding event counts. (only if there is point pattern data)

**Author(s)**

Craig Wang

**See Also**

[fusion](#), [fusion.dstan](#)

**Examples**

```
# three responses with a single latent Gaussian process
if (require("geoR", quietly = TRUE) & require("SDraw", quietly = TRUE)) {
dat1 <- fusionSimulate(n.point = 100, n.area = 10, n.grid = 2,
  psill = 1, phi = 1, nugget = 0, tau.sq = 0.5,
  point.beta = list(rbind(1,5)), area.beta = list(rbind(-1, 0.5)),
  distributions = c("normal", "poisson"), pp.offset = 0.1,
  design.mat = matrix(c(1,1,1)))
}

# three responses with two latent Gaussian processes
dat2 <- fusionSimulate(n.point = 100, n.area = 10, n.grid = 2,
  psill = c(1,2), phi = c(2,1), nugget = c(0,0), tau.sq = 1,
```

```
point.beta = list(rbind(1,5)), area.beta = list(rbind(-1, 0.5)),
distributions = c("normal","poisson"), pp.offset = 0.1,
design.mat = matrix(c(1,1,1,2,3,4), ncol = 2))
```

---

plot

*Generate diagnostics plot for a fusion model*


---

### Description

Plot model diagnostics for fusionModel objects. By default, it shows posterior versus prior distributions of fixed effect coefficients and latent parameters. The names of fixed effect coefficients are covariate names followed by internal parameter names in parentheses. 'beta\_p' denotes the coefficients for point data and 'beta\_a' denotes the coefficients for lattice data.

### Usage

```
## S3 method for class 'fusionModel'
plot(x, posterior = TRUE, interactive = TRUE, ...)
```

### Arguments

x	object of class fusionModel. Output of <code>fusion()</code> .
posterior	logical. If TRUE, then shows posterior versus prior distributions of fixed effect coefficients and latent parameters.
interactive	logical. If TRUE, then print messages in the terminal to proceed to next plots.
...	additional arguments not used

### Details

When `posterior = FALSE`, then traceplot of posterior samples for the fixed effect coefficients and latent parameters are shown for Stan approach and the mesh overlayed with spatial data is shown for INLA approach.

### Author(s)

Craig Wang

### Examples

```
## example based on simulated data
## Not run:
if (require("INLA", quietly = TRUE) & require("SDraw", quietly = TRUE)) {
  dat <- fusionSimulate(n.point = 20, n.area = 10, n.grid = 2,
    psill = 1, phi = 1, nugget = 0, tau.sq = 0.5,
    point.beta = list(rbind(1,5)),
    area.beta = list(rbind(-1, 0.5)),
    distributions = c("normal","poisson"),
```

```

design.mat = matrix(c(1,1,1))

geo_data <- data.frame(x = dat$mrf[dat$sample.ind, "x"],
                      y = dat$mrf[dat$sample.ind, "y"],
                      cov.point = dat$data$X_point[,2],
                      outcome = dat$data$Y_point[[1]])
lattice_data <- sp::SpatialPolygonsDataFrame(dat$poly,
      data.frame(outcome = dat$data$Y_area[[1]],
      cov.area = dat$data$X_area[,2]))

dat_inla <- fusionData(geo.data = geo_data, geo.formula = outcome ~ cov.point,
                      lattice.data = lattice_data, lattice.formula = outcome ~ cov.area,
                      pp.data = dat$data$lgcp.coords[[1]], distributions = c("normal", "poisson"),
                      method = "INLA")

mod_inla <- fusion(data = dat_inla, n.latent = 1, bans = 0,
                  prior.range = c(1, 0.5), prior.sigma = c(1, 0.5),
                  mesh.locs = dat_inla$locs_point, mesh.max.edge = c(0.5, 1))

plot(mod_inla, interactive = FALSE)
}

## End(Not run)

```

---

predict

*Obtain predictions for the latent processes of spatial fusion model*


---

## Description

Generate posterior values containing predictions of the latent Gaussian process(es) based on a fitted spatial fusion model and new locations.

## Usage

```

## S3 method for class 'fusionModel'
predict(object, new.locs, type = c("summary", "full"), ...)

```

## Arguments

object	an object of class <code>fusionModel</code> . Output of <code>fusion()</code> .
new.locs	<code>data.frame</code> , <code>SpatialPoints</code> or <code>SpatialPointsDataFrame</code> . Contains the locations where the latent process(es) will be predicted. If <code>data.frame</code> , it must have column names "x" and "y" as coordinates of observations.
type	string, The default "summary" gives posterior median of latent process(es); "full" gives full marginals (for INLA) or posterior samples (for Stan) of latent process(es).
...	additional arguments not used

**Value**

The returned value is a list containing the posterior values for the latent spatial components.

For INLA models, the output represents the latent components that are associated with each response variable multiplied by the design matrix  $Z$ . They are indexed with  $ij$ , where  $i$  denotes the  $i$ th latent process and  $j$  denotes the  $j$ th variable. The variables are ordered by geostatistical, lattice, point pattern data.

For Stan models, the output represents the original latent components before multiplied by the design matrix  $Z$ . Each spatial component is indexed with  $i$ , where  $i$  denotes the  $i$ th latent process.

**Author(s)**

Craig Wang

**Examples**

```
## example based on simulated data
## Not run:
if (require("INLA", quietly = TRUE) & require("SDraw", quietly = TRUE)) {
  dat <- fusionSimulate(n.point = 20, n.area = 10, n.grid = 2,
    psill = 1, phi = 1, nugget = 0, tau.sq = 0.5,
    point.beta = list(rbind(1,5)),
    area.beta = list(rbind(-1, 0.5)),
    distributions = c("normal", "poisson"),
    design.mat = matrix(c(1,1,1)))

  geo_data <- data.frame(x = dat$mrf[dat$sample.ind, "x"],
    y = dat$mrf[dat$sample.ind, "y"],
    cov.point = dat$data$X_point[,2],
    outcome = dat$data$Y_point[[1]])
  lattice_data <- sp::SpatialPolygonsDataFrame(dat$poly,
    data.frame(outcome = dat$data$Y_area[[1]],
    cov.area = dat$data$X_area[,2]))

  dat_inla <- fusionData(geo.data = geo_data, geo.formula = outcome ~ cov.point,
    lattice.data = lattice_data, lattice.formula = outcome ~ cov.area,
    pp.data = dat$data$lgcp.coords[[1]],
    distributions = c("normal", "poisson"), method = "INLA")

  mod_inla <- fusion(data = dat_inla, n.latent = 1, bans = 0,
    prior.range = c(1, 0.5), prior.sigma = c(1, 0.5),
    mesh.locs = dat_inla$locs_point, mesh.max.edge = c(0.5, 1))

  pred_inla <- predict(mod_inla, dat$pred.loc, type = "summary")
}

## End(Not run)
```

summary

*Obtain summary of parameter estimates for a spatial fusion model***Description**

Generate summary statistics for posterior parameter estimates from a spatial fusion model.

**Usage**

```
## S3 method for class 'fusionModel'
summary(object, digits = 3, ...)
```

**Arguments**

object	object of class fusionModel. Output of <code>fusion()</code> .
digits	integer. The number of significant digits.
...	additional arguments not used.

**Value**

The returned value is a matrix containing the parameter estimates and their summary statistics. The names of fixed effect coefficients are covariate names followed by internal parameter names in parentheses. 'beta\_p' denotes the coefficients for point data and 'beta\_a' denotes the coefficients for lattice data.

**Author(s)**

Craig Wang

**Examples**

```
## example based on simulated data
## Not run:
if (require("INLA", quietly = TRUE) & require("SDraw", quietly = TRUE)) {
  dat <- fusionSimulate(n.point = 20, n.area = 10, n.grid = 2,
    psill = 1, phi = 1, nugget = 0, tau.sq = 0.5,
    point.beta = list(rbind(1,5)),
    area.beta = list(rbind(-1, 0.5)),
    distributions = c("normal", "poisson"),
    design.mat = matrix(c(1,1,1)))

  geo_data <- data.frame(x = dat$mrf[dat$sample.ind, "x"],
    y = dat$mrf[dat$sample.ind, "y"],
    cov.point = dat$data$X_point[,2],
    outcome = dat$data$Y_point[[1]])

  lattice_data <- sp::SpatialPolygonsDataFrame(dat$poly,
    data.frame(outcome = dat$data$Y_area[[1]],
    cov.area = dat$data$X_area[,2]))
```

```
dat_inla <- fusionData(geo.data = geo_data, geo.formula = outcome ~ cov.point,
  lattice.data = lattice_data, lattice.formula = outcome ~ cov.area,
  pp.data = dat$data$lgcp.coords[[1]],
  distributions = c("normal","poisson"), method = "INLA")

mod_inla <- fusion(data = dat_inla, n.latent = 1, bans = 0,
  prior.range = c(1, 0.5), prior.sigma = c(1, 0.5),
  mesh.locs = dat_inla$locs_point, mesh.max.edge = c(0.5, 1))

summary(mod_inla)
}

## End(Not run)
```

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