

Package ‘SBmedian’

August 16, 2021

Type Package

Title Scalable Bayes with Median of Subset Posteriors

Version 0.1.1

Description Median-of-means is a generic yet powerful framework for scalable and robust estimation. A framework for Bayesian analysis is called M-posterior, which estimates a median of subset posterior measures. For general exposition to the topic, see the paper by Minsker (2015) <[doi:10.3150/14-BEJ645](https://doi.org/10.3150/14-BEJ645)>.

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Encoding UTF-8

Imports Rcpp, Rdpack, expm, stats, utils

LinkingTo Rcpp, RcppArmadillo

RoxygenNote 7.1.1

RdMacros Rdpack

NeedsCompilation yes

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Repository CRAN

Date/Publication 2021-08-16 07:10:05 UTC

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mpost.euc

Median Posterior for Subset Posterior Samples in Euclidean Space

Description

mpost.euc is a general framework to *merge* multiple empirical measures $Q_1, Q_2, \dots, Q_M \subset R^p$ from independent subset of data by finding a median

$$\hat{Q} = \operatorname{argmin}_Q \sum_{m=1}^M d(Q, Q_m)$$

where Q is a weighted combination and $d(P_1, P_2)$ is distance in RKHS between two empirical measures P_1 and P_2 . As in the references, we use RBF kernel with bandwidth parameter σ .

Usage

```
mpost.euc(
  splist,
  sigma = 0.1,
  maxiter = 121,
  abstol = 1e-06,
  show.progress = FALSE
)
```

Arguments

splist	a list of length M containing vectors or matrices of univariate or multivariate subset posterior samples respectively.
sigma	bandwidth parameter for RBF kernel.
maxiter	maximum number of iterations for Weiszfeld algorithm.
abstol	stopping criterion for Weiszfeld algorithm.
show.progress	a logical; TRUE to show iteration mark, FALSE otherwise.

Value

a named list containing:

med.atoms a vector or matrix of all atoms aggregated.

med.weights a weight vector that sums to 1 corresponding to med.atoms.

weiszfeld.weights a weight for M subset posteriors.

weiszfeld.history updated parameter values. Each row is for iteration, while columns are weights corresponding to weiszfeld.weights.

References

Minsker S, Srivastava S, Lin L, Dunson DB (2014). “Scalable and Robust Bayesian Inference via the Median Posterior.” In *Proceedings of the 31st International Conference on International Conference on Machine Learning - Volume 32*, ICML’14, II–1656–II–1664. event-place: Beijing, China.

Minsker S, Srivastava S, Lin L, Dunson DB (2017). “Robust and Scalable Bayes via a Median of Subset Posterior Measures.” *Journal of Machine Learning Research*, **18**(124), 1–40. <https://jmlr.org/papers/v18/16-655.html>.

Examples

```
## Median Posterior from 2-D Gaussian Samples
# Step 1. let's build a list of atoms whose numbers differ
set.seed(8128) # for reproducible results
mydata = list()
mydata[[1]] = cbind(rnorm(96, mean= 1), rnorm(96, mean= 1))
mydata[[2]] = cbind(rnorm(78, mean=-1), rnorm(78, mean= 0))
mydata[[3]] = cbind(rnorm(65, mean=-1), rnorm(65, mean= 1))
mydata[[4]] = cbind(rnorm(77, mean= 2), rnorm(77, mean=-1))

# Step 2. Let's run the algorithm
myrun = mpost.euc(mydata, show.progress=TRUE)

# Step 3. Visualize
# 3-1. show subset posterior samples
opar <- par(no.readonly=TRUE)
par(mfrow=c(2,3), no.readonly=TRUE)
for (i in 1:4){
  plot(mydata[[i]], cex=0.5, col=(i+1), pch=19, xlab="", ylab="",
        main=paste("subset",i), xlim=c(-4,4), ylim=c(-3,3))
}

# 3-2. 250 median posterior samples via importance sampling
id250 = base::sample(1:nrow(myrun$med.atoms), 250, prob=myrun$med.weights, replace=TRUE)
sp250 = myrun$med.atoms[id250,]
plot(sp250, cex=0.5, pch=19, xlab="", ylab="",
      xlim=c(-4,4), ylim=c(-3,3), main="median samples")

# 3-3. convergence over iterations
matplot(myrun$weiszfeld.history, xlab="iteration", ylab="value",
        type="b", main="convergence of weights")
par(opar)
```

Description

SPD manifold is a collection of matrices that are symmetric and positive-definite and it is well known that using Euclidean geometry for data on the manifold is rather inaccurate. Here, we propose a function for dealing with SPD matrices specifically where valid examples include full-rank covariance and precision matrices. Note that $N_M = \sum_{m=1}^M n_m$.

Usage

```
mpost.spd(
  splist,
  sigma = 0.1,
  maxiter = 121,
  abstol = 1e-06,
  show.progress = FALSE
)
```

Arguments

splist a list of length M containing $(p \times p)$ matrix or 3d array of size $(p \times p \times n_m)$ whose slices are SPD matrices from subset posterior samples respectively.

sigma bandwidth parameter for RBF kernel.

maxiter maximum number of iterations for Weiszfeld algorithm.

abstol stopping criterion for Weiszfeld algorithm.

show.progress a logical; TRUE to show iteration mark, FALSE otherwise.

Value

a named list containing:

med.atoms a $(p \times p \times N_M)$ 3d array whose slices are atoms aggregated.

med.weights a weight vector that sums to 1 corresponding to med.atoms.

weiszfeld.weights a weight for M subset posteriors.

weiszfeld.history updated parameter values. Each row is for iteration, while columns are weights corresponding to weiszfeld.weights.

Examples

```
## Median Posterior from 5-dimension Wishart distribution
## Visualization will be performed for distribution of target eigenvalue
## where RED is for estimated density and BLUE is density from all samples.

# Step 1. let's build a list of atoms whose numbers differ
set.seed(8128) # for reproducible results
mydata = list()
mydata[[1]] = stats::rWishart(96, df=10, Sigma=diag(5))
mydata[[2]] = stats::rWishart(78, df=10, Sigma=diag(5))
mydata[[3]] = stats::rWishart(65, df=10, Sigma=diag(5))
mydata[[4]] = stats::rWishart(77, df=10, Sigma=diag(5))
```

```

# Step 2. Let's run the algorithm
myrun = mpost.spd(mydata, show.progress=TRUE)

# Step 3. Compute largest eigenvalues for the samples
eig4 = list()
for (i in 1:4){
  spd mats = mydata[[i]]      # SPD atoms
  spds size = dim(spd mats)[3] # number of atoms
  eigvals = rep(0,spds size)  # compute largest eigenvalues
  for (j in 1:spds size){
    eigvals[j] = max(base::eigen(spd mats[,j])$values)
  }
  eig4[[i]] = eigvals
}
eigA = unlist(eig4)
eiglim = c(min(eigA), max(eigA))

# Step 4. Visualize
# 4-1. show distribution of subset posterior samples' eigenvalues
opar <- par(no.readonly=TRUE)
par(mfrow=c(2,3))
for (i in 1:4){
  hist(eig4[[i]], main=paste("subset", i), xlab="largest eigenvalues",
       prob=TRUE, xlim=eiglim, ylim=c(0,0.1))
  lines(stats::density(eig4[[i]]), lwd=1, col="red")
  lines(stats::density(eigA), lwd=1, col="blue")
}

# 4-2. 250 median posterior samples via importance sampling
id250 = base::sample(1:length(eigA), 250, prob=myrun$med.weights, replace=TRUE)
sp250 = eigA[id250]
hist(sp250, main="median samples", xlab="largest eigenvalues",
     prob=TRUE, xlim=eiglim, ylim=c(0,0.1))
lines(stats::density(sp250), lwd=1, col="red")
lines(stats::density(eigA), lwd=1, col="blue")

# 4-3. convergence over iterations
matplot(myrun$weiszfeld.history, xlab="iteration", ylab="value",
       type="b", main="convergence of weights")
par(opar)

```

Description

Median-of-means is a generic yet powerful framework for scalable and robust estimation. A framework for Bayesian analysis is called M-posterior, which estimates a median of subset posterior measures.

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